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Evaluation of $\text{SF}_6$, $\text{C}_2\text{Cl}_4$, and $\text{CO}$ to approximate fossil fuel $\text{CO}_2$ in the Northern Hemisphere using a chemistry transport model

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[1] The distribution of the fossil fuel component in atmospheric $\text{CO}_2$ cannot be measured directly at a cheap cost. Could anthropogenic tracers with source patterns similar to fossil fuel $\text{CO}_2$ then be used for that purpose? Here we present and evaluate a methodology using surrogate tracers, $\text{CO}$, $\text{SF}_6$, and $\text{C}_2\text{Cl}_4$, to deduce fossil fuel $\text{CO}_2$. A three-dimensional atmospheric chemistry transport model is used to simulate the relationship between each tracer and fossil fuel $\text{CO}_2$. In summertime the regression slopes between fossil fuel $\text{CO}_2$ and surrogate tracers show large spatial variations for chemically active tracers ($\text{CO}$ and $\text{C}_2\text{Cl}_4$), although $\text{C}_2\text{Cl}_4$ presents less scatter than $\text{CO}$. At two tall tower sites in the United States (WLEF, Wisconsin, and WITN, North Carolina), we found that in summertime the $\text{C}_2\text{Cl}_4$ ($\text{CO}$) versus fossil $\text{CO}_2$ slope is on average up to 15% (25%) higher than in winter. We show that for $\text{C}_2\text{Cl}_4$ this seasonal variation is due to $\text{OH}$ oxidation. For $\text{CO}$ the seasonal variation is due to both chemistry and mixing with nonanthropogenic CO sources. In wintertime the three surrogate tracers $\text{SF}_6$, $\text{C}_2\text{Cl}_4$, and $\text{CO}$ are about equally as good indicators of the presence of fossil $\text{CO}_2$. However, our model strongly underestimates the variability of $\text{SF}_6$ at both towers, probably because of unaccounted for emissions. Hence poor knowledge of emission distribution hampers the use of $\text{SF}_6$ as a surrogate tracer. From a practical point of view we recommend the use of $\text{C}_2\text{Cl}_4$ as a proxy of fossil $\text{CO}_2$. We also recommend the use of tracers to separate fossil $\text{CO}_2$. Despite the fact that the uncertainty on the regression slope is on the order of 30%, the tracer approach is likely to have less bias than when letting one model with one inventory emission map calculate the fossil $\text{CO}_2$ distribution.


1. Introduction

[2] This paper investigates the role of ancillary tracers in helping to determine the fossil fuel component of atmospheric $\text{CO}_2$. Fossil fuel emissions are the largest term of the human induced perturbation of the global carbon cycle, and they drive the long-term increase of atmospheric $\text{CO}_2$. Annual totals of fossil fuel emissions for the globe have errors estimated to be 6–10% [Marland and Rotty, 1984]. The average national emission total has perhaps a 8% uncertainty associated with it. However, uncertainties may range from −340% to 90% for a given country and year [Andres et al., 1999]. Also, the space and time pattern of fossil fuel emissions, is more uncertain than the emission country totals. Generally, human population density, for example, is used to distribute the country totals, ignoring or simplifying patterns of energy use and energy production, such as electricity generation from fuel burning, habitat heating and cooking, and transportation. When applying atmospheric inversions to $\text{CO}_2$ concentrations measurements, fossil fuel fluxes are rarely sought in their own right. They are rather constrained separately from terrestrial or oceanic sources or sinks. The most common approach consists in calculating, with a transport model, the atmospheric $\text{CO}_2$ gradients due to fossil fuel emissions, and then subtracting this signal from station observations to invert the residual natural fluxes over different regions. Doing so propagates two kinds of systematic errors in the inversions. First, using a fixed a priori pattern of fossil fuel emissions might generate errors in ascribing fluxes to the biosphere and the oceans rather than to the fixed fossil fuel emissions. Second, transport models have biases in simulating the time varying distribution of fossil fuel $\text{CO}_2$ (FF$\text{CO}_2$) in the atmosphere. Those biases are unknown because there is (almost) no direct measurement of FF$\text{CO}_2$, but a lower limit of those biases can be recognized by taking the spread...
between different transport model results. Gurney et al. [2004] found for instance that transport model differences are on the order of 20% in simulating fossil CO₂ response functions at two tall towers in the United States.

[3] In order to quantify the fossil fuel component of the CO₂ concentration, it is tantalizing to use measurements of ancillary tracers that relate to FFCO₂. The best ancillary analogue of fossil CO₂ is likely to be radiocarbon-CO₂ or \( ^{14}\text{CO₂} \). The spatial gradients of \( ^{14}\text{CO₂} \) in the Northern Hemisphere reflect the dilution of radiocarbon-free FFCO₂ in radiocarbon rich ambient air. Radiocarbon-CO₂ measurements with sufficiently high precision are however costly and labor intensive and cannot be deployed as routine measurements on a large network of stations, nor be taken with high enough sampling frequency [Levin et al., 2003]. Therefore other anthropogenic tracers are needed with emissions patterns as close as possible to those of fossil CO₂ and which could be measured at relatively moderate costs. Bakwin et al. [1998], for example, used carbon monoxide (CO) to subtract the contribution of fossil sources to total CO₂ at tall towers in the United States. Zondervan and Meijer [1996] measured the relationship between \( ^{14}\text{CO₂} \) and CO in Netherlands in order to “calibrate” CO as a surrogate for fossil CO₂ during pollution episodes. The underlying idea is here to establish an empirical calibration between the ancillary tracer and fossil CO₂, either locally or regionally, and then apply it to isolate fossil CO₂ from total CO₂ atmospheric observations.

[4] Our goal is to test the capability of different tracers to quantify the distribution of FFCO₂ in the atmosphere. These tracers are CO₂, SF₆, and C₂Cl₄. The reason for testing CO is that it is emitted together with FFCO₂ during the combustion of fuels. Complications may arise however from the fact that CO is destroyed by OH with an average lifetime of 2 months whereas fossil CO₂ is inert, and that CO has other sources than FFCO₂ (wild fires and oxidation of biogenic hydrocarbons). The reason for testing SF₆ and C₂Cl₄ is that those tracers are anthropogenic, and to first order, their emissions are distributed similarly to those of FFCO₂. SF₆ is inert and C₂Cl₄ has an atmospheric lifetime with respect to oxidation by OH of less than 6 months [Prather et al., 2001].

[5] We will proceed in three steps. First, in the absence of systematic \( ^{14}\text{CO₂} \) measurements everywhere to establish the relationship between FFCO₂ and ancillary tracers, we use a transport model to map the spatial variations in that relationship in the Northern Hemisphere. Second, we analyze the temporal relationships between modeled FFCO₂ and each tracer at two tall tower stations in the United States, where continuous observations of the tracers exist and can be used to verify the model predictions. Third, based on model results, we estimate the different errors associated with the use of tracers to isolate the fossil fuel component of CO₂. After describing the transport model and the emission maps (section 3), we map the regression slopes between FFCO₂ and each ancillary tracer (section 4). In section 5, we investigate the temporal variability of the correlation between fossil CO₂ and tracers on synoptic timescales at two tall tower sites in North Carolina (WITN) and Wisconsin (WLEF). We use actual in situ tracer data to compare them to model results. In section 6, we discuss the different errors associated with the proxy tracer method to estimate FFCO₂ from model-derived regressions.

2. Problem

[6] Critical to using ancillary tracers for quantifying the fossil fuel component of CO₂ is the error introduced in the method. Let \( X_f \) be the observed CO₂ concentration at a station, \( X_a \) the unknown fossil fuel component, and \( X_m \) the measured tracer concentration. One can write that

\[
X_f = X_f + X_x, \quad (1)
\]

where \( X_x \) is the “residual” CO₂ concentration from the terrestrial and oceanic surface fluxes. We seek to determine \( X_x \), for instance for inverting its gradients into regional natural sources and sinks. A common way to do this is to model \( X_f \) at each site, and replace unknown \( X_f \) by a simulated value \( X_{sim} \). The model bias versus reality is unknown, but a lower bound to model error of \( X_{sim} \) can be approximated from the spread of different transport model realizations. The TRANSCOM3 project compared 13 global transport models using the same prescribed emission maps of FFCO₂. Results showed differences on monthly mean \( X_{sim} \) concentrations of up to 3 ppm at Northern Hemisphere atmospheric stations.

[7] For using an ancillary tracer to isolate the fossil CO₂ component, we consider that the sources of \( X_x \) and those of fossil CO₂ are reasonably collocated and proportional to each other. The atmospheric transport and chemistry processes will thus also produce roughly proportional concentration fields. Hence one can deduce \( X_f \) from \( X_a \) with a linear model, rewriting equation (1) as

\[
X_f = X_f + S(x, t)X_x, \quad (2)
\]

where \( X_x \) is the measured concentration of the ancillary tracer, and \( S \) the regression slope between tracer and fossil CO₂. Ideally, one would need to know an “instantaneous” slope \( S(x, t) \) at each site and each time, which is impossible to obtain by observations. A reasonable hypothesis is that experimentalists can measure the slope \( S \) for example on a few episodes, at a few representative stations, and then extrapolate the value of \( S \) to isolate fossil CO₂ elsewhere. A coarser method is to determine \( S \) from the ratio of inventoried emissions, and then assume that \( S \) is conserved in the transport process. This latter assumption would work only if the \( X_f \) to \( X_a \) emissions ratio was uniform in space and time, and if \( X_a \) is a passive tracer.

[8] We present here a model-based design study for quantifying \( S(x, t) \) and evaluating the different errors in isolating fossil CO₂ using an ancillary tracer. The sources of errors that we aim to quantify relate to the spatial variability of \( S(x, t) \) in the atmosphere, to the temporal variability of \( S(x, t) \), to uncertainties in \( S \) and to measurement errors in \( X_m \) (see equation (1)). Given that, we can assess whether the tracer based approach is more valuable than using a model to transport fossil emissions and separate \( X_f \) as done in current inversions. We investigate the use of CO, SF₆, and C₂Cl₄, all being routinely measured together with CO₂, either on a continuous basis at a few sites in the United States, or at many more flask sampling sites. To do so, we
model the time varying concentration of these tracers and of fossil CO$_2$ using an atmospheric chemistry transport model. We first model the variations of $S$ over the Northern Hemisphere. Second, we model the variability of $S$ at two tall tower sites in the United States where the model can be evaluated against in situ CO, SF$_6$ and C$_2$Cl$_4$ observations. The modeled deviations from an idealized perfect linear relationship between $X_a$ and $X_f$ are used to evaluate uncertainties in $S$, and from there, uncertainties in the overall inference of the fossil CO$_2$ using modeled slopes and measured CO, SF$_6$ and C$_2$Cl$_4$ concentrations.

3. Modeling Framework

3.1. Atmospheric Chemistry Transport Model

[9] We model the time-varying concentrations of fossil CO$_2$, CO, SF$_6$, and C$_2$Cl$_4$ taking into account transport and, if necessary, OH chemistry. To that list, we add a conceptual tracer called pC$_2$Cl$_4$, which has the same sources as C$_2$Cl$_4$, but remains chemically inert in the model. We use the LMD$_2$-INCA transport model. LMD$_2$ is an atmospheric general circulation model developed initially for climate studies [Sadourny and Laval, 1984]. The model has been adapted in order to simulate the transport of trace species [Hourdin and Armengaud, 1999] and it is coupled online to the chemistry aerosols model: Interaction with Chemistry and Aerosols (INCA). A detailed description and evaluation of the LMD$_2$-INCA model is given by Hauglustaine et al. [2004]. Model intercomparison involving LMD$_2$-INCA can be found in the work of Bauer et al. [2004], Brunner et al. [2003, 2005], Guibert et al. [2005], and Roelofs et al. [2003].

[10] We use an online version of the LMDz-INCA with 19 hybrid levels from the surface up to 3 hPa. The vertical resolution is of about 300–500 m in the planetary boundary layer (first level at 70 m height). The model horizontal resolution is 2.5° in latitude and 3.75° in longitude. The large-scale advection of tracers is performed using the finite volume transport scheme of Van Leer [1977] as described by Hourdin and Armengaud [1999]. Convective transport is simulated using the mass flux scheme of Tiedke [1989]. The planetary boundary layer scheme is based on a second-order closure approximation. The horizontal model winds are relaxed toward ECMWF reanalyzed winds (nudged) with a relaxation time of 2.5 hours.

[11] The version of the INCA chemical scheme used in this study describes the methane oxidation cycle including 19 photochemical reactions and 62 chemical reactions. The INCA module calculates online the time evolution of 33 species with a time step of 20 min. In the present version of the model, nonmethane hydrocarbons and the feedback of the chemistry on the radiation are not taken into account. Hauglustaine et al. [2004] evaluated the transport chemistry model against different sets of observations, and concluded that OH was overestimated in the model by 19% to 25% due to these limitations. We carry out a 1 year spin-up for the LMD$_2$-INCA chemistry transport model before producing mixing ratio output. The analysis is made for an arbitrary year (1998).

3.2. Surface Emissions

[12] Surface FFCO$_2$ emissions are from the EDGAR version 3.2 inventory for year 1995 [Olivier and Berdowski, 2001]. FFCO$_2$ is injected in the lowest box of the atmosphere model (0–140 m). These emissions have no diurnal and no seasonal variation, although we know that, over some regions, there is a seasonality, on the order of 20% in some regions in Germany and of 15% over the United States, for example [Levin et al., 2001; Blasing et al., 2005], due to different use of fossil fuels for heating or air conditioning.

[13] Surface or near surface sources of CO are the sum of fossil fuel and technological biofuel combustion, biomass burning and nonmethane hydrocarbons oxidation. We use fossil fuel CO emissions for year 1995 from EDGAR version 3.2 with global emissions rescaled to the global inventoried totals of 1998 given by Prather et al. [2001]. Since nonmethane hydrocarbons (NMHC) are not explicitly included in our chemistry transport model, secondary CO produced by these short-lived species is treated as a surface source, as by Shindell et al. [2001]. The global amount of secondary CO produced by NMHC is taken from Prather et al. [2001] and distributed with the pattern of the EDGAR 3.2 fossil CO emissions for anthropogenic NMHC and with the pattern of Guenther et al. [1995] isoprene emissions for biogenic NMHC. The ratio of secondary CO over primary CO emissions is $\approx$30%. Biomass burning CO emissions are based on emission factors compiled by Andreae and Merlet [2001], and fire distributions of Hao and Liu [1994] in the tropics and of Müller [1992] in the extratropics. The spatial and temporal distribution of CO oceanic emissions is taken from Erickson and Taylor [1992] and scaled to a global mean of 50 Tg CO/yr. More information on the prescribed CO emissions can be found in the work of Hauglustaine et al. [2004].

[14] The SF$_6$ emissions are geographically distributed according to electrical power usage estimated from the UN Energy statistics yearbook 1992 by country and population density (5’ population map of CIESIN). A major source of SF$_6$ is its use as a dielectric insulator in high-voltage electrical switches. We scale the global mean SF$_6$ emission total to a global yearly value of 5.686 Gg/yr given by Levin and Hesshaimer [1996], and assumed no seasonal cycle of emissions.

[15] The C$_2$Cl$_4$ emission map was originally created for year 1990, based upon regional sales data available on a continental scale, national gross domestic products, and population density patterns. C$_2$Cl$_4$ is used as a dry cleaning agent in industrial and commercial activities, and it has an atmospheric lifetime with respect to oxidation by OH of less than 6 months [Prather et al., 2001]. Since C$_2$Cl$_4$ emissions have been declining after the Montreal Protocol, we scaled globally the 1990 emissions by a factor of 0.82 to extrapolate the global emission inventory for year 1998 following the linear curve given by McCulloch et al. [1999]. The C$_2$Cl$_4$ emissions are assumed to be temporally invariant over each grid point. In the chemistry transport model we let C$_2$Cl$_4$ be oxidized by OH at the rate $k = K_0 \exp(-1200/T)$ with $K_0 = 9.4 \times 10^{-12}$ cm$^3$/(mol s) [De More et al., 1997].

4. Mapping: Spatial Variations in the Ratios of Fossil CO$_2$ to the Ancillary Tracers

4.1. Mapping the Ratios of Emissions

[16] We show in Figures 1b–1d the spatial distribution of the normalized ratios $\rho(x,y)$ of the emissions of fossil CO$_2$ to
each tracer normalized. For CO emissions, we used the sum of primary sources only. The normalized ratio in each grid point of the Northern Hemisphere is defined by

\[
\rho_i = \frac{F_i(x, y)}{\sum_{NH} F_i} \Bigg/ \frac{F_f(x, y)}{\sum_{NH} F_f},
\]

where \(F_i(x, y)\) is the emission of the tracer \(i\) on grid point \((x, y)\) and \(F_f(x, y)\) the emission of fossil CO\(_2\) at the same location. With the normalization, one would have uniform values of \(\rho(x, y) = 1\) everywhere for a tracer with emissions perfectly collocated with those of fossil CO\(_2\). Spatial patterns in \(\rho\) as shown in Figures 1b–1d indicate regional deviations from the average Northern Hemisphere emission ratio of fossil CO\(_2\) for each tracer emissions. Once transported, such deviations induce spatial and temporal variations in the correlations between the mixing ratios of tracers and fossil CO\(_2\). In Figure 1, the ratios of CO, SF\(_6\) or C\(_2\)Cl\(_4\) to fossil CO\(_2\) emissions have, over the United States, a spread between the lowest (\(\rho \approx 0.4\)) and highest (\(\rho \approx 1.9\)) values of \(\rho\) that is less than on other continents (Europe and Asia). The fossil CO\(_2\) to C\(_2\)Cl\(_4\) ratios show over Europe an interesting pattern with higher values of (\(\rho \approx 1.9\)) in the east and lower values in the west (\(\rho \approx 0.3\)). The rest of Eurasia has values of the fossil CO\(_2\) to C\(_2\)Cl\(_4\) ratios greater than one (Figure 1c). The fossil CO\(_2\) to SF\(_6\) ratio map shows contrasting differences between China (\(\rho \approx 2\)) and India where the values are closer to one (Figure 1d). The fossil CO\(_2\) to primary CO sources ratios in Figure 1b show low values (\(\rho \approx 0.2\)) in the tropics and in boreal regions due to biomass burning sources which rise the flux of CO without

Figure 1. (a) FFCO\(_2\) emission map. Units are 1.10\(^9\) mol/m\(^2\)/s. (b–d) Normalized ratios \(\rho_i\) as defined in the text, where \(i = \text{CO (Figure 1b), C}_2\text{Cl}_4\) (Figure 1c), and SF\(_6\) (Figure 1d). The \(\rho_i\) are ratios of the sources of FFCO\(_2\) to CO, C\(_2\)Cl\(_4\), and SF\(_6\) normalized by the North Hemisphere totals so that they can be compared to one. The ratios are saturated at a value of 2. These figures exhibit spatial differences in the emissions maps between FFCO\(_2\) and the surrogate tracers.
changing fossil CO$_2$ fluxes. Ratios of FFCO$_2$ to CO emissions are however fairly uniform over Europe and the United States.

4.2. Mapping the Ratios of Concentrations

[17] We sampled the model simulated total CO, C$_2$Cl$_4$, SF$_6$ and FFCO$_2$ fields at a time step of 20 min over each grid point. We performed linear regression of the ancillary tracer concentrations against FFCO$_2$ for each month. In calculating linear regression slopes for time series that are serially correlated, we accounted for autocorrelation in time, using the time domain analysis of Bakwin et al. [1997, method 4]. This provides more realistic uncertainty estimates than if atmospheric variability is assumed uncorrelated. The autocorrelative regression slopes between the concentrations of tracer, $X_i$ and $X_f$, are computed using

$$S_H = \frac{C_f + dc_f}{C_i + dc_i},$$

where $C_H$ is the covariance between tracers $i$ and fossil CO$_2$ at time lag of $\Delta$, as given by

$$C_H(\Delta) = \sum_t \hat{X}_f(t)Y_i(t + \Delta),$$

where $Y(t)$ is the detrended concentration time series with diurnal and seasonal cycles removed, normalized by emissions over the Northern Hemisphere and $\hat{X}_f(t)$ is the time series of simulated fossil CO$_2$. The overbar indicates averaging over $\Delta = 4$–30 hours. The terms $dc_H$ are each 1000 random values selected from a normal distribution with mean zero and a standard deviation equal to the standard deviations between lags 61–480 hours of the covariance of the time series at the given point.

[18] The autocorrelative slopes are mapped in Figure 2 for August and in Figure 3 for December. We can compare concentration regression slopes (Figure 2) with emission ratios (Figure 1) between fossil CO$_2$ and ancillary tracers.

Figure 2. Map of the normalized autocorrelation regression slopes relating the four surrogate tracers SF$_6$, CO, C$_2$Cl$_4$, and pC$_2$Cl$_4$ to FFCO$_2$ for the month of August.
Different scales of coherence are seen between the two maps, with concentration regression slopes being spatially coherent at scales of 5000 km versus a few hundred km for the emission ratio maps. In August, higher OH concentrations decrease CO and C$_2$Cl$_4$ concentrations relative to FFCO$_2$ and thus make the slopes higher than in December. The average slopes and their standard deviation over the United States, North Atlantic and Europe are given in Table 1. We found the largest spatial gradients in the slope in summer and for the chemically active species (Table 1). The August spatial gradients of FFCO$_2$ versus CO and C$_2$Cl$_4$ slopes are two times smaller over Europe than over North America, reflecting the spatial structure of underlying emission ratios (Figure 1). Comparing in Figures 2a–2c the slopes for C$_2$Cl$_4$ and pC$_2$Cl$_4$ shows the influence of chemistry in summer. Chemistry induces on average, four times

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**Table 1.** Mean and Standard Deviation of the Slopes Between Tracers and Fossil CO$_2$ Over North America, North Atlantic, and Europe in January and August

<table>
<thead>
<tr>
<th></th>
<th>North America</th>
<th>North Atlantic</th>
<th>Europe</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Jan</td>
<td>Aug</td>
<td>Jan</td>
</tr>
<tr>
<td>CO</td>
<td>1.3 (0.2)</td>
<td>1.5 (0.7)</td>
<td>1.3 (0.2)</td>
</tr>
<tr>
<td>SF$_6$</td>
<td>0.8 (0.2)</td>
<td>0.8 (0.1)</td>
<td>0.8 (0.1)</td>
</tr>
<tr>
<td>C$_2$Cl$_4$</td>
<td>0.7 (0.2)</td>
<td>1.1 (0.5)</td>
<td>0.7 (0.1)</td>
</tr>
<tr>
<td>pC$_2$Cl$_4$</td>
<td>0.7 (0.1)</td>
<td>0.8 (0.1)</td>
<td>0.7 (0.1)</td>
</tr>
</tbody>
</table>
larger spatial gradients in the FF CO2 versus C2Cl4 slopes compared to the FF CO2 versus pC2Cl4 ones.

5. Mapping Temporal Variations in the Correlations of Tracers FF CO2 Versus the Tracers at Two Tall Towers in the United States

In this section, we further analyze correlation between ancillary tracers and FF CO2 at two tall tower sites where in situ tracer observations exist. Doing so, we still rely on model calculations of fossil CO2, but we can now evaluate the modeled tracer concentrations against real observations.

5.1. Tall Tower Measurements in North Carolina and Wisconsin

Tracer data are from the North Carolina (WITN) and Wisconsin (WLEF) tall towers operated by NOAA/CMDL. The WITN tower is 610 m tall, located in a rural area of the eastern United States at 35.37°N, 77.39°W, relatively close, to industrialized regions of the east coast. The WLEF tower is 447 m tall and is located in a forested and sparsely populated region of northern Wisconsin at 45.95°N, 90.27°W, 472 m asl [Bakwin et al., 1995, 1998]. Of particular interest is the contrast of population around the two towers, with 64 persons km−2 at WITN and 5 persons km−2 at WLEF (typical density of regions within 50 km or more of the towers) [Bakwin et al., 1998]. Generally, the WLEF tower samples air masses containing the integrated signals of distant source regions, mixed with cleaner regional background air, whereas the WITN tower is more immediately influenced by anthropic emissions.

In summer at WITN (Figure 5), SF6 is the modeled tracer with the highest correlation coefficient with fossil CO2 ($R^2 = 0.997$). The second best correlation with fossil CO2 is found with C2Cl4 ($R^2 = 0.981$). We obtain a lower correlation than for SF6 due to the removal of C2Cl4 by OH. The conceptual passive tracer (pC2Cl4), exhibits in contrast a correlation with fossil CO2 of 0.996, equally as good as for SF6. In August, scatter around the linear fit to the regression of C2Cl4 versus fossil CO2 in Figure 5 owes to the fact that each “polluted” air mass carries a distinct ratio between C2Cl4 and fossil CO2, with OH increasing the fossil CO2 to C2Cl4 ratio. Finally, CO shows the worst correlation with fossil CO2 ($R^2 = 0.905$). This occurs because CO is destroyed by OH, and CO has sources not collocated with fossil CO2 emissions, such as biomass burning and production from NMHC. The same conclusions relative to which tracer best approximates fossil CO2 also hold at the WLEF tall tower. In Wisconsin, the correlation of CO versus fossil CO2 ($R^2 = 0.805$) is lower than in North Carolina ($R^2 = 0.905$). The WLEF tower is reached in summer by air masses with elevated CO originating from wildfires in Canada and the western United States and low fossil CO2 concentrations. For both tower sites, the modeled correlations between CO, C2Cl4 and fossil CO2 are higher in December than in August. This is primarily due to inhibited OH chemistry increasing the lifetime of active tracers. In fact, we find that in December, all ancillary tracers SF6, C2Cl4 and CO are about equally as good indicators of the presence of fossil CO2. Potosnak et al. [1999] reached to a similar conclusion for CO and fossil CO2 based on atmospheric records from the Harvard Forest (Massachusetts). At WLEF, the winter correlations between any tracer and fossil CO2 are always lower than at WITN in North Carolina. Located closer to anthropogenic emissions, the WITN tower remains more consistently influenced by regional emissions from the east coast. We recall from Figure 1 that different industrialized regions of the Northern Hemisphere have SF6 to fossil CO2 emission ratios that can vary by a factor of two. In winter, the signals from those different regions get mixed by fast longitudinal transport, and no unambiguous surrogate tracer of fossil CO2 can be obtained. This is a major limitation of using tracers to isolate the fossil fuel signal in the CO2 concentration field, which has been overlooked when using for example, a slope simply derived from regional emission inventories [Bakwin et al., 1995].

5.2. Variability of the Fossil CO2 Versus Tracer Scatterplots

In Figures 4 and 5, we show fossil CO2 versus each modeled tracers regression plots in August and December. At WITN, we find a tighter correlation for both winter and summer than at WLEF. This is likely due to the fact that there is a good collocation among the proximate sources of all species. Relying on the model to evaluate tracers for isolating fossil CO2, this result clearly indicates that the method to establish a proxy for fossil CO2 tends to be site specific. Generally better correlations will be expected at sites downwind from emission regions. At face value, we expect any tight relationship between FF CO2 and tracers to degrade if a station is placed very close to a source region (i.e., in a city) because of averaging at the grid level. Indeed, Gerbig et al. [2003] showed that past a model grid size of 30 km the representation error (due to averaging of the subgrid variability) greatly dominates the actual sampling error (coming from the atmospheric variance) of CO2 measurements. Thus variance induced by the close proximity of the sources will not be captured in a global transport model such as LMDZ-INCA but rather will increase the representation error.

5.3. Variability of the Fossil CO2 Versus Tracer Regression Slopes

The monthly linear regression slope of fossil CO2 versus SF6 remains approximately constant throughout the year at both towers (Figure 6). This indicates that, according
to our model, SF₆ should be both a spatially and temporally robust proxy for fossil CO₂. The SF₆ versus fossil CO₂ slope is close to 1 at WITN and equal to 0.9 at WLEF, a difference which can be explained by the larger influence of remote sources at WLEF, characterized by lower FFCO₂ to SF₆ ratios.

[25] The monthly slope between C₂Cl₄ and fossil CO₂ is not constant throughout the year, as is the case for SF₆. This
is mainly because $\text{C}_2\text{Cl}_4$ is affected by reaction with OH, as can be inferred from comparison between $\text{pC}_2\text{Cl}_4$ and $\text{C}_2\text{Cl}_4$. In Figure 6 at WLEF, the comparison between the $\text{pC}_2\text{Cl}_4$ and $\text{C}_2\text{Cl}_4$ slopes shows that the oxidation by OH changes the slopes from being equal in winter to differ by 15% over the summer months when OH photochemical production is maximum (the difference is slightly less than 10% at WITN due to the closer proximity to the sources). This raises a caution flag if $\text{C}_2\text{Cl}_4$ is to be used like a passive tracer for isolating the fossil CO$_2$ component. Oxidation by OH tends to make the fossil CO$_2$ versus $\text{C}_2\text{Cl}_4$ slope higher than the fossil CO$_2$ versus $\text{pC}_2\text{Cl}_4$ slope. Similarly to SF$_6$, we found that the fossil CO$_2$ versus $\text{C}_2\text{Cl}_4$ normalized slope is lower at WLEF, owing to dilution of air masses of...
different origin into background air containing more C2Cl4 in proportion to FFCO2. For chemically reactive species, differences among sites can be explained both by differences in exposure to OH (more OH increases the slope), and by differences in mixing with background air (more dilution with background air high in C2Cl4 decreases the slope).

[26] The monthly regression slope of fossil CO2 versus CO is on average 20% higher than the idealized value of 1 if both tracers had identical sources and transport. Other primary sources of CO than fossil fuel combustion would otherwise tend to decrease the fossil CO2 versus CO slope. Our results indicate that the effect of photochemical destruction of CO is more important in controlling the value of the slope. In addition, the effect of OH is proportionally larger on the fossil CO2 versus CO slope than on that for fossil CO2 versus C2Cl4 because CO has a shorter lifetime than C2Cl4. This hinders the use of an annually constant slope for using CO to subtract the fossil component of CO2 observations in North America. Using a slope value predicted by a chemistry transport model might be a feasible alternative, provided that the model performs well in reproducing the variations of CO. Inspecting the monthly linear correlation coefficient of fossil CO2 versus CO in the model shows that CO may be safely used to approximate fossil CO2 between October and February, but that it is not a reliable proxy during the rest of the year. Comparing the correlation coefficients values at WLEF and WITN does not favor either station.

5.4. Modeled Variance of Tracers

[27] Deducing FFCO2 from ancillary tracers using model derived regression slopes, raises the key question of whether or not the model captures the variability of actual tracer data. In the next section, we compare modeled and observed tracer concentrations at the two tall towers and discuss the implications of model-data mismatch for determining the fossil CO2 component.

[28] Modeled and observed tracers time series for the year 1998 are shown in Figure 7 (WITN) and Figure 8 (WLEF). At both towers, a seasonal cycle for CO and C2Cl4 is present, but weaker at WITN. WITN lies closer to the sources so that CO and C2Cl4 are less oxidized by OH. In contrast to CO and C2Cl4, SF6 does not show any seasonal cycle. There is no seasonality prescribed to the emissions of C2Cl4, thus the modeled C2Cl4 seasonal cycle only reflects transport and varying OH concentrations. This is not the case for CO, which has a biomass burning component maximum in summer [Hao and Liu, 1994]. The proximity of anthropogenic sources explains why there is a greater variability at WITN than at WLEF both in the model and in the observations (Table 2).

[29] Synoptic variability is an important determinant of the value of the slopes. Thus it is important to show that the model correctly captures this mode of variability. Figure 9 displays tracer changes during the first 3 months of 1998 at WITN. Most synoptic events appear well correlated across all tracers suggesting good collocation of the sources for these compounds. Figure 9 shows good (>0.5) correlation between model and data for CO and C2Cl4 but the magnitude and the phase of SF6 changes are not well captured.

[30] We compare in Table 2 the modeled and observed tracer variability, in standard deviation of hourly values. The model underestimates the observed standard deviation by a factor four for SF6 at both towers whereas the simulated CO and C2Cl4 are realistic. These results for SF6 should not reduce our confidence in the model which works well for CO and C2Cl4.

[31] Compared to the model intercomparison of Denning et al. [1999] (Figure 8), the LMDz simulated variability measured as the difference between the third and first quartile is 0.21 ppt for WITN and 0.14 ppt for WLEF which puts LMDz among the best half of the models. SF6 mixing ratios seem to be influenced by non inventoried local sources (at least at the two towers). Also the relative measurement error (Table 3) is the largest for SF6 when compared to CO or C2Cl4, which could partly explain why models are less able to capture the hourly variability of SF6.

[32] In terms of error on the slope, a model underestimation of the variance by a factor of four would propagate into multiplying the error on the slope (cf next section) by the same amount. Unfortunately, this precludes the use of SF6 and model-derived slopes to determine FFCO2, even though...
in the model realm, the SF₆ slopes were found the most robust (see section 4.3).

6. Analysis of Errors and Discussion

[33] To further assess the accuracy of the method by which fossil CO₂, X_f can be deduced from a tracer X_a by X_f = SX_a (see equations (1) and (2)), we give in Table 3 the measurement error on X_a and the uncertainty on the slope S at both tower locations.

[34] The reported measurement errors for each tracer are relative errors, (instrument precision errors divided by observed standard deviation of each species). Care has to be taken in computing uncertainties in the slope S in the model. The concentrations being autocorrelated in time, a simple RMS fit error from the linear fit X_f versus X_a would greatly underestimate the true error as can be seen in Table 3, by comparing the RMS fit error and the slope uncertainty. In Table 3, slope uncertainty values are determined as half the range between the 16th and 84th percentiles of the Monte Carlo estimates of the slopes computed using equation (4) (uncertainty bars shown at the bottom of Figure 6). It is important to keep in mind that our slope uncertainty which accounts for serial correlation in the time series, is related to variability not explained by the correlations and gives more reliable uncertainty estimates than other methods [Bakwin et al., 1997]. The uncertainty on the slope of the order 30 to 40% is clearly the dominant source of error in the approximation X_f = SX_a. The measurement errors are always at least a factor two smaller than the uncertainty on the slope.

[35] Other systematic errors enter in the tracer approximation of FFCO₂. Emission fluxes are biased by aggregation errors in space and time. However, aggregation errors associated with tightly constrained spatial patterns in the emission maps may cancel since similar aggregation errors are likely to bias FFCO₂ and anthropogenic tracer emissions. To evaluate the impact of seasonality in FFCO₂ emissions slopes, we performed the same model analysis using a FFCO₂ emission map with a prescribed peak to peak seasonality of 20% in the Northern Hemisphere (maximum emissions in winter). Results of this test for
the two tall towers (not shown) showed a reduction of the modeled slopes in summer and an overall annual bias of 20% when compared with the case of invariant sources of FFCO$_2$.

[36] This analysis of the uncertainty associated with the ancillary tracer method is important in assessing its practical use. The “standard method” in CO$_2$ inversions is to subtract the fossil fuel component of the CO$_2$ concentration at stations out of the observed CO$_2$. The fossil CO$_2$ component is estimated using one particular emission inventory maps and one particular transport model. The inversion then solves for “residual” oceanic and terrestrial fluxes. The strategy in using a tracer method consists in deriving fossil fuel concentrations from tracers observations with modeled slopes. We showed that the main source of uncertainty on the slope $S$ is on the order 30%. In the standard method a large part of the uncertainty is contained in the (unknown) bias of the transport model. Using several models can provide a measure of this error. The spread between different global transport models is on the order of 20% in simulating monthly fossil CO$_2$ at the two tall towers WLEF and WITN [Gurney et al., 2004]. This is probably a lower bound of the model uncertainty since (1) the same smooth emission map was prescribed to all models and (2) only coarse-scale global models were used. So, the conditions

**Figure 8.** Same as Figure 7 but at WLEF. Monthly normalized regression slopes for WLEF (Wisconsin) and WITN (North Carolina) computed when accounting for autocorrelations in time series (see text). A perfect proxy of FFCO$_2$ should have at any month a slope close to 1. In black are the SF$_6$-FFCO$_2$ slopes, in red are the CO-FFCO$_2$ slopes, in blue are the C$_2$Cl$_4$-FFCO$_2$ slopes, and in green are the C$_2$Cl$_4$-p-FFCO$_2$ slopes. Error bars shown at the bottom of the plot correspond to half the range between the 16th and 84th percentiles of the Monte Carlo estimates of the slopes (see text).

**Table 2.** Standard Deviation of the Detrended Time Series and Comparison Between the Observations and the Modeled Time Series

<table>
<thead>
<tr>
<th>Species</th>
<th>WLEF</th>
<th>WITN</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Observed</td>
<td>Modeled</td>
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<tr>
<td>CO</td>
<td>32</td>
<td>24</td>
</tr>
<tr>
<td>SF$_6$</td>
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<td>0.05</td>
</tr>
<tr>
<td>C$_2$Cl$_4$</td>
<td>2.6</td>
<td>2.8</td>
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</tbody>
</table>

*For all species the variability is greater at the WITN (North Carolina) tower. Units are ppt for SF$_6$ and C$_2$Cl$_4$ and ppb for CO.
of the intercomparison did not allow to explore all the range of model differences. Error associated with regional patterns in emissions are also expected to be significant. At the national level, for fossil CO$_2$, total emissions is known with an error of 8% uncertainty, but it can range from −340% to 90% for a given country and year [Andres et al., 1999]. Emissions are obtained by making the product of an emission factor by an activity. There are significant sources of errors due to activity definitions, activity mapping, and to the use of emission factors determined for one region/activity and used for another. Hence the spatial distribution of fossil emissions at regional scales is even more uncertain than country totals. Also, only recently has the seasonality of the emissions and potential associated error been considered in inversions [Gurney et al., 2004]. When using refined fossil fuel emissions, with hourly temporal variation over Europe at a 50 km resolution, it appears that the spread of the model increased significantly (P. Peylin and CarboEurope-IP participants, preliminary results).

[37] The tracer method is likely to be more robust than the standard method. The errors associated with transport and emissions tend to be smaller in the tracer approach since ratios of two tracers are used with the same model (thus canceling some of the modeled transport bias) and using emission sources which can share common biases (e.g., activity distributions). Thus the errors on the ratio used to

### Table 3. Relative Errors$^a$

<table>
<thead>
<tr>
<th></th>
<th>Fit Error</th>
<th>Measurement Error</th>
<th>Slope Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<td>Aug</td>
<td>DJF</td>
</tr>
<tr>
<td>CO</td>
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<tr>
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<tr>
<td>C$_2$Cl$_4$</td>
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<td>WITN</td>
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<tr>
<td>pC$_2$Cl$_4$</td>
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</tr>
<tr>
<td>WITN</td>
<td>1.9</td>
<td>2.3</td>
<td>35</td>
</tr>
</tbody>
</table>

$^a$Expressed in percent. See text for a description of the different errors.
quantify fossil CO\textsubscript{2} are less impacted by biases than in the standard method.

7. Conclusion

[38] Using an atmospheric chemistry transport model, we simulated the regression slope between fossil CO\textsubscript{2} and the one of anthropogenic tracers CO, SF\textsubscript{6} and C\textsubscript{2}Cl\textsubscript{4}. One can then use this slope to estimate fossil CO\textsubscript{2} from actual measurement of surrogate tracers. We evaluated the model using actual tracer observations at two tall towers sites in the United States. We estimated the regression slopes variations in the Northern Hemisphere, and the errors in the retrieval of fossil CO\textsubscript{2} based upon anthropogenic tracers.

[39] The fossil CO\textsubscript{2} to CO and C\textsubscript{2}Cl\textsubscript{4} ratio is smaller over Europe than over North America, reflecting difference in emissions. The regression slopes show larger spatial variations in summer than in winter for the reactive tracers CO and C\textsubscript{2}Cl\textsubscript{4}, which reflects their removal by OH radicals. We compared two tall tower sites (WLEF, Wisconsin and WITN, North Carolina) in the United States. We found that differences in the ratio of fossil CO\textsubscript{2} versus tracers between the two sites can be explained both by differences in exposure to OH (more active OH photochemistry increases the ratio), and by differences in their proximity to pollution (more polluted air decreases the ratio). The regression slopes of fossil CO\textsubscript{2} to tracers vary during the year. The largest values occur in summer for the chemically reactive species CO (+25\%) and C\textsubscript{2}Cl\textsubscript{4} (+15\%). This raises a caution flag if C\textsubscript{2}Cl\textsubscript{4} or CO are assumed to be passive tracers for retrieving the fossil CO\textsubscript{2} component. At the two tall tower sites, our model results indicate that the effect of CO removal by OH is more important in controlling the value of the slope than mixing with nonanthropogenic CO. In addition, the impact of OH removal on the slope is proportionally larger on the fossil CO\textsubscript{2} versus CO slope than on the fossil CO\textsubscript{2} versus C\textsubscript{2}Cl\textsubscript{4} one. This is because CO has a shorter lifetime than C\textsubscript{2}Cl\textsubscript{4}. In wintertime, all anthropogenic tracers SF\textsubscript{6}, C\textsubscript{2}Cl\textsubscript{4} and CO are about equally as good proxies of fossil CO\textsubscript{2}.

[40] When we compared modeled to observed variance of the mixing ratios, we found that the model underestimates the observed standard deviation by a factor of four for SF\textsubscript{6} at both towers whereas results for CO and C\textsubscript{2}Cl\textsubscript{4} are good. We believe that this is due to SF\textsubscript{6} mixing ratios being very dependent on local and point sources (at least for the two towers) that are not included in the model. In the end, this precludes the use of SF\textsubscript{6} in this method at least in comparison to CO and C\textsubscript{2}Cl\textsubscript{4} even though in the “modeled world,” SF\textsubscript{6} slopes were more robust in terms of time and space variability. Thus among SF\textsubscript{6}, CO, C\textsubscript{2}Cl\textsubscript{4}, we recommend C\textsubscript{2}Cl\textsubscript{4} since it has less spatial and time variability than CO and since SF\textsubscript{6} variability is not correctly captured by the model. The uncertainty on the slope S of fossil CO\textsubscript{2} versus tracer, is estimated to be on the order of 30 to 40%. Uncertain S values are the dominant cause of error when retrieving fossil CO\textsubscript{2} from tracer concentration measurements. Traditionally in atmospheric inversions, the fossil CO\textsubscript{2} component is subtracted out of the modeled CO\textsubscript{2} mixing ratio to solve for residual ocean and terrestrial sources and sinks. In that process, Fossil CO\textsubscript{2} emission inventory maps, input to transport models are used to compute the fossil CO\textsubscript{2} signal. The errors on this approach include transport model errors and emission inventories errors. The spread from 16 different transport models [Gurney et al., 2004] suggests that a lower bound on the transport error is on the order of 20\%, but models can all remain biased with respect to the unknown truth. The spread from different emission inventories maps is also likely to be quite large, on the order of 30–40\% locally (P. Peylin and Carboeurope-IP participants, preliminary results). Errors on emission inventories are small at global scale but largely increase down to regional scale. In the tracer method studied here, using model-derived slopes, the errors associated with transport or emission inventories will tend to cancel each other since the ratios of two tracers are estimated using the same model and emission maps can share common biases through the distribution of anthropogenic activities. Monthly values of the ratio between fossil CO\textsubscript{2} and each anthropogenic tracer can be of interest for experimentalists who could determine the value these slopes only at a few sites. Information on the space and time variability in the ratios could hence be used to assess the representativeness of slopes measured at a given point. Using tabulated values of these ratios would improve on practices where a constant ratio is used during the whole year as done in the past with CO for example. Finally, a natural follow up of this work is to use the tracer method in inversions to reduce uncertainties on fossil fuel CO\textsubscript{2} fluxes.

References


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